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**Space-time adaptive FIR filtering with staggered PRI**

# **Space-Time Adaptive FIR filtering with staggered PRI**

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## Report Documentation Page

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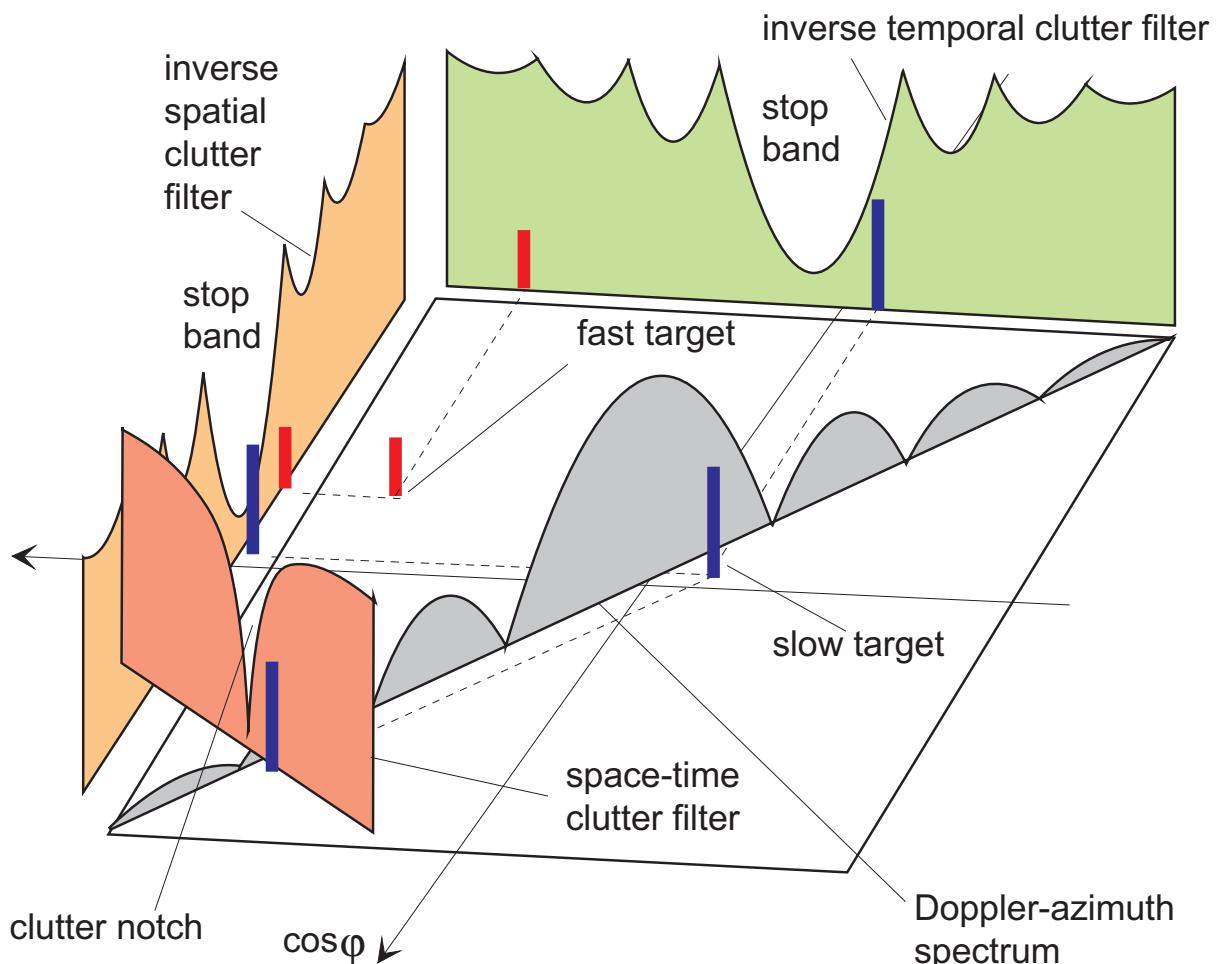
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## **Space-time adaptive FIR filtering with staggered PRI**

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## Space-time adaptive FIR filtering with staggered PRI



Principle of STAP

clutter spectrum    temporal filter    spatial filter    STAP

## Principle of STAP

**Space-time adaptive FIR filtering with staggered PRI**

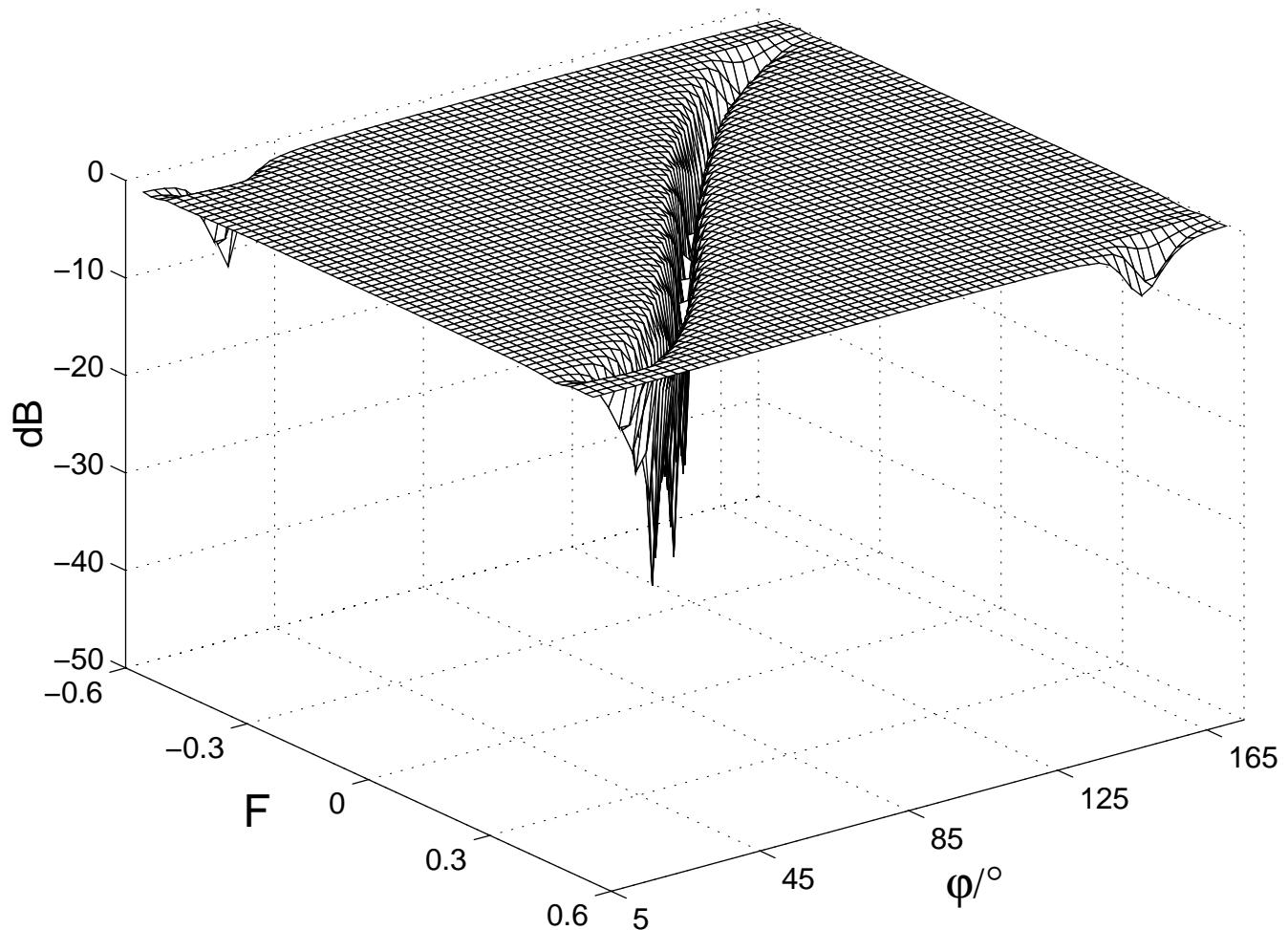
## The optimum processor

$$\mathbf{w} = a \mathbf{Q}^{-1} \mathbf{s}(j, v)$$

**Q** space-time clutter+noise covariance matrix  
**s** space-time steering vector

For large dimensions  $N, M$  not realizable by various reasons  
(amount of computations, lack of training data, accuracy)

## Space-time adaptive FIR filtering with staggered PRI



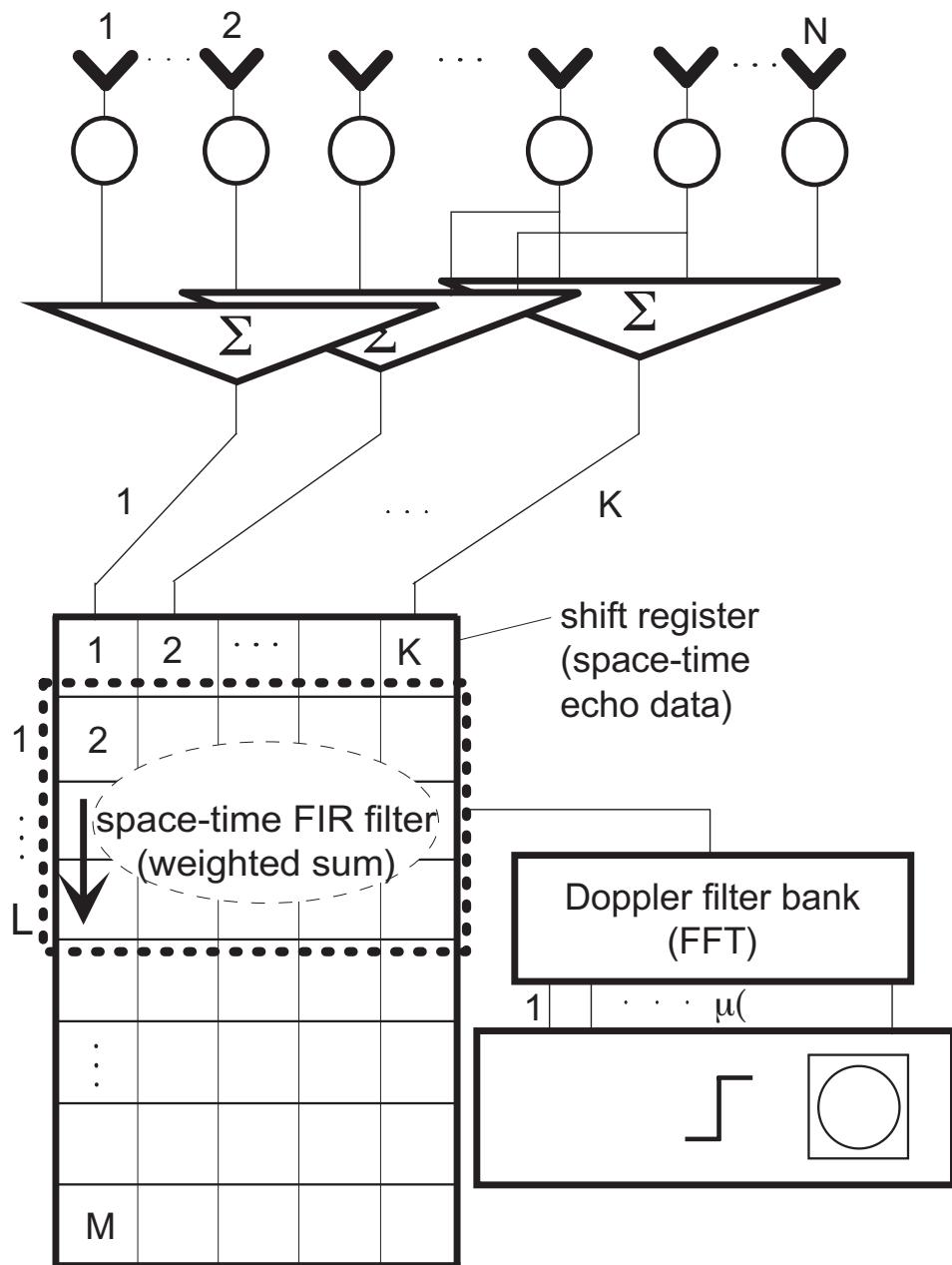
Azimuth-Doppler Characteristics of a  
STAP Filter for Sidelooking Array

## **Space-time adaptive FIR filtering with staggered PRI**

### **Subspace STAP techniques**

- Space-time transforms (e.g. GSC concepts)
- Spatial transforms (reduction in the spatial dimension)
- **FIR filters** (reduction in the temporal dimension, => very efficient solution)
- Multi-stage filters
- Frequency dependent spatial processing (for large CPI only)
- Angle-Doppler subgroups (e.g. JDL-GLRT)
- others

## Space-time adaptive FIR filtering with staggered PRI



Overlapping subarray processor with  
space-time FIR filter

**Space-time adaptive FIR filtering with staggered PRI**

$$\mathbf{Q} = \begin{pmatrix} \mathbf{Q}_{11} & \mathbf{Q}_{12} & \cdots & \mathbf{Q}_{1M} \\ \mathbf{Q}_{21} & \mathbf{Q}_{22} & \cdots & \mathbf{Q}_{2M} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{Q}_{M1} & \mathbf{Q}_{M2} & \cdots & \mathbf{Q}_{MM} \end{pmatrix}$$

The space-time clutter+noise covariance matrix

$$\mathbf{K} = \mathbf{Q}^{-1} = \begin{pmatrix} \mathbf{K}_{11} & \mathbf{K}_{12} & \cdots & \mathbf{K}_{1M} \\ \mathbf{K}_{21} & \mathbf{K}_{22} & \cdots & \mathbf{K}_{2M} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{K}_{M1} & \mathbf{K}_{M2} & \cdots & \mathbf{K}_{MM} \end{pmatrix}$$

and its inverse

**Space-time adaptive FIR filtering with staggered PRI**

$$\mathbf{K} = \mathbf{Q}^{-1} = \begin{pmatrix} \mathbf{K}_{11} & \mathbf{K}_{12} & \cdots & \mathbf{K}_{1L} \\ \mathbf{K}_{21} & \mathbf{K}_{22} & \cdots & \mathbf{K}_{2L} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{K}_{L1} & \mathbf{K}_{L2} & \cdots & \mathbf{K}_{LL} \end{pmatrix}$$

The north-west  $NL \times NL$  submatrix  
( $N$  number of antenna elements,  $L$  temporal filter length)

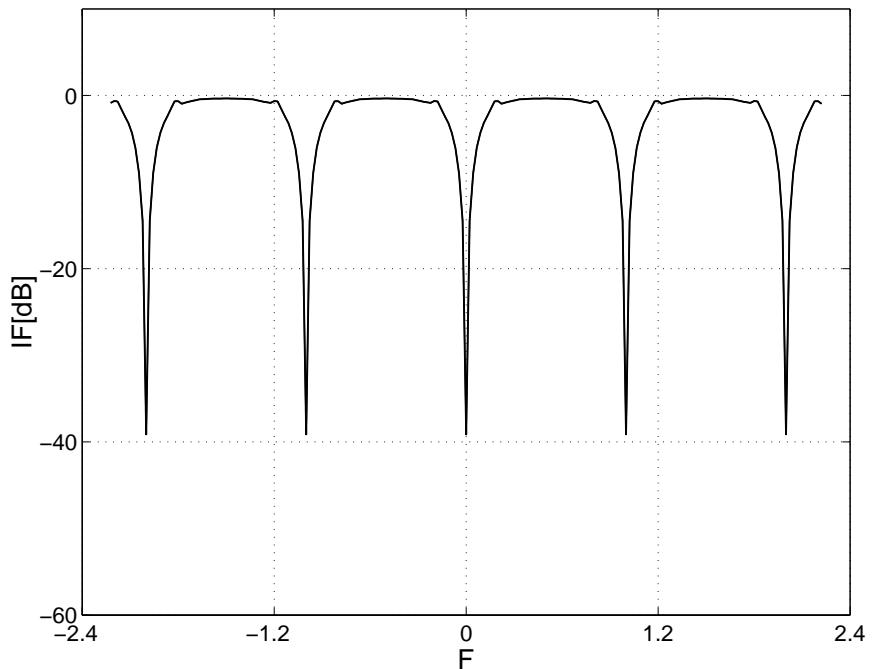
$$\tilde{\mathbf{K}} = \begin{pmatrix} \mathbf{K}_{11} \\ \mathbf{K}_{21} \\ \vdots \\ \mathbf{K}_{L1} \end{pmatrix}$$

The LS FIR filter matrix (1. Block column of inverse)

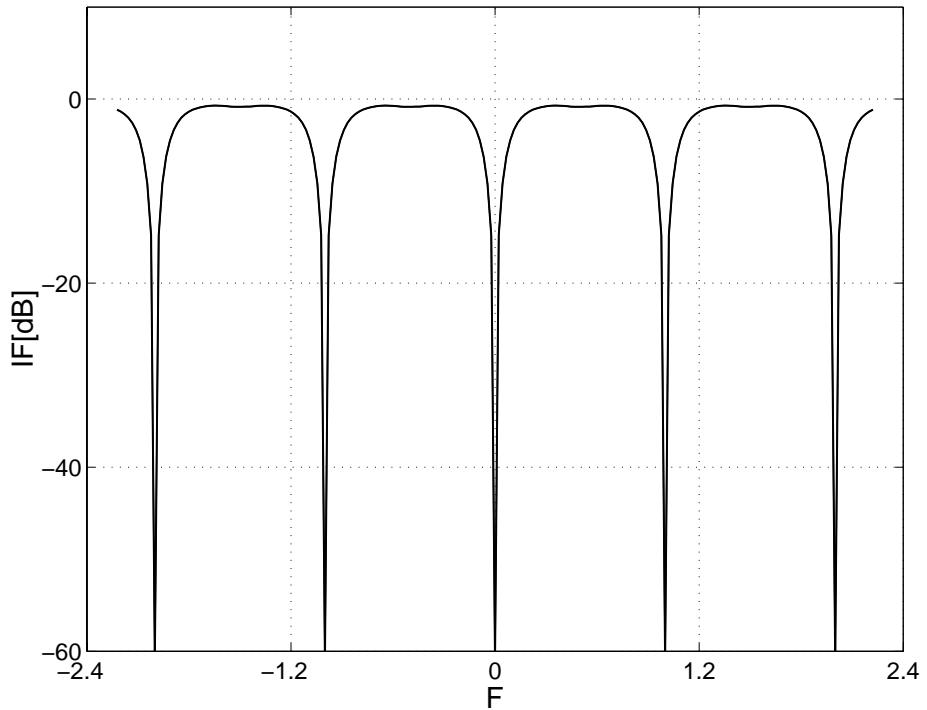
$$\mathbf{h} = \tilde{\mathbf{K}} \mathbf{b}$$

Further reduction: beamforming

## Space-time adaptive FIR filtering with staggered PRI

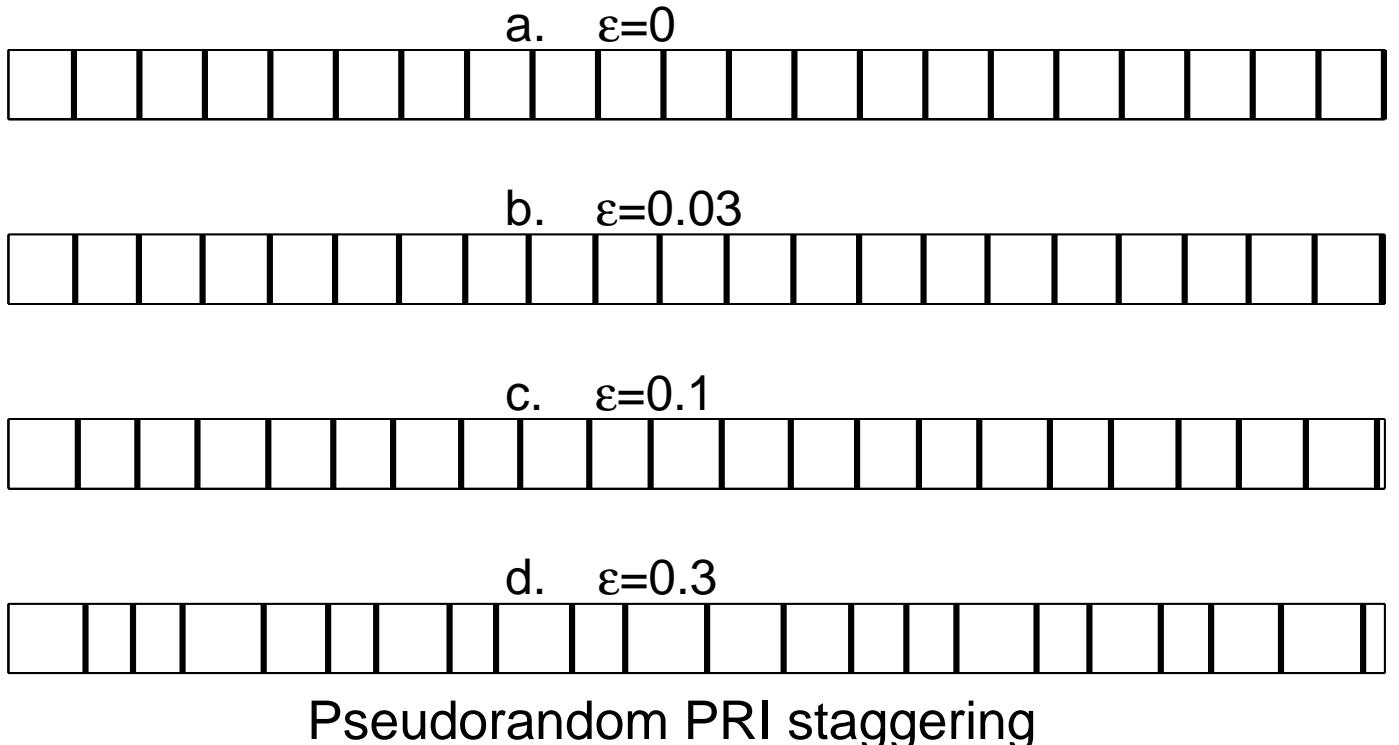


Fully adaptive processing, constant PRI



FIR filter, 5 taps, constant PRI

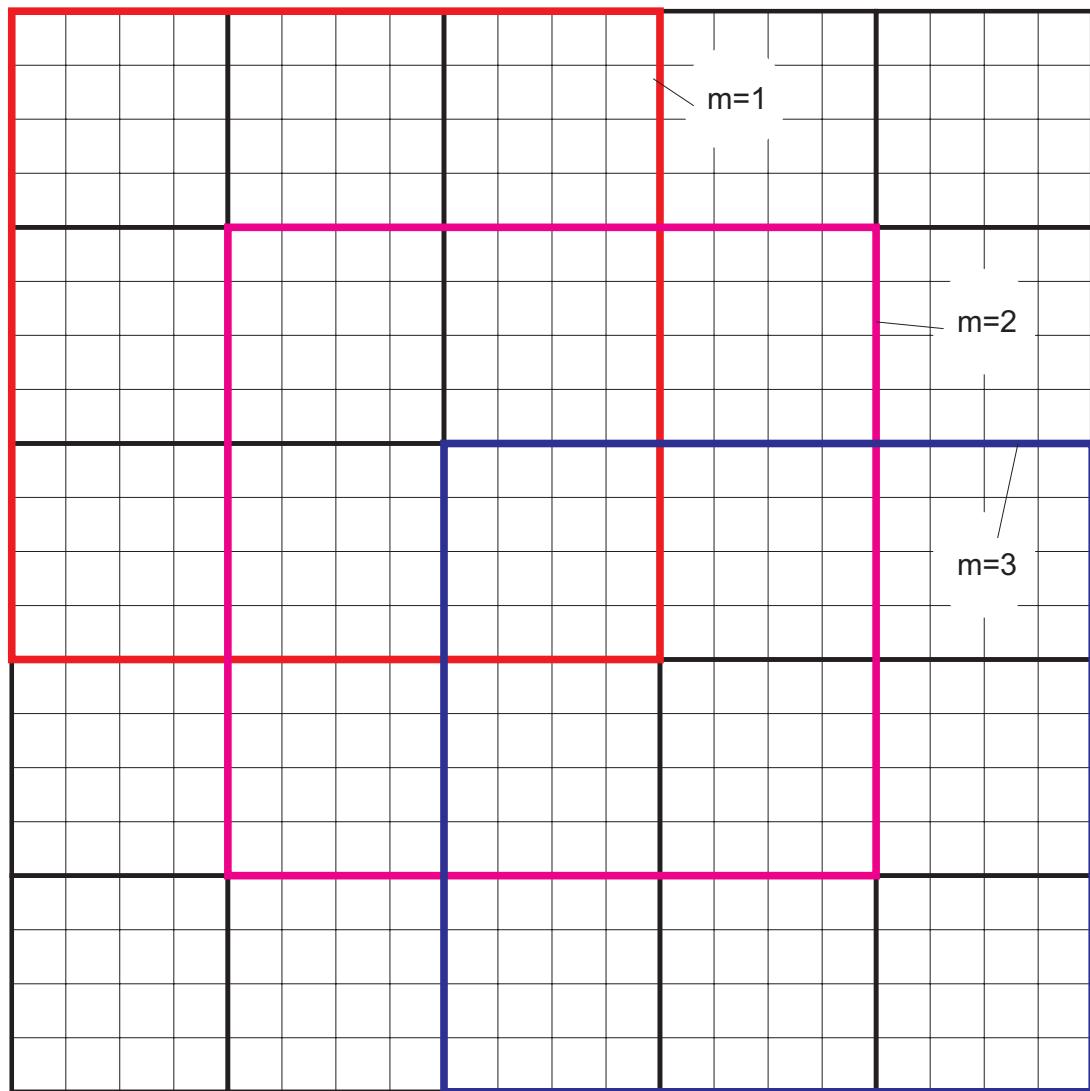
## Space-time adaptive FIR filtering with staggered PRI



## Properties of staggered PRI

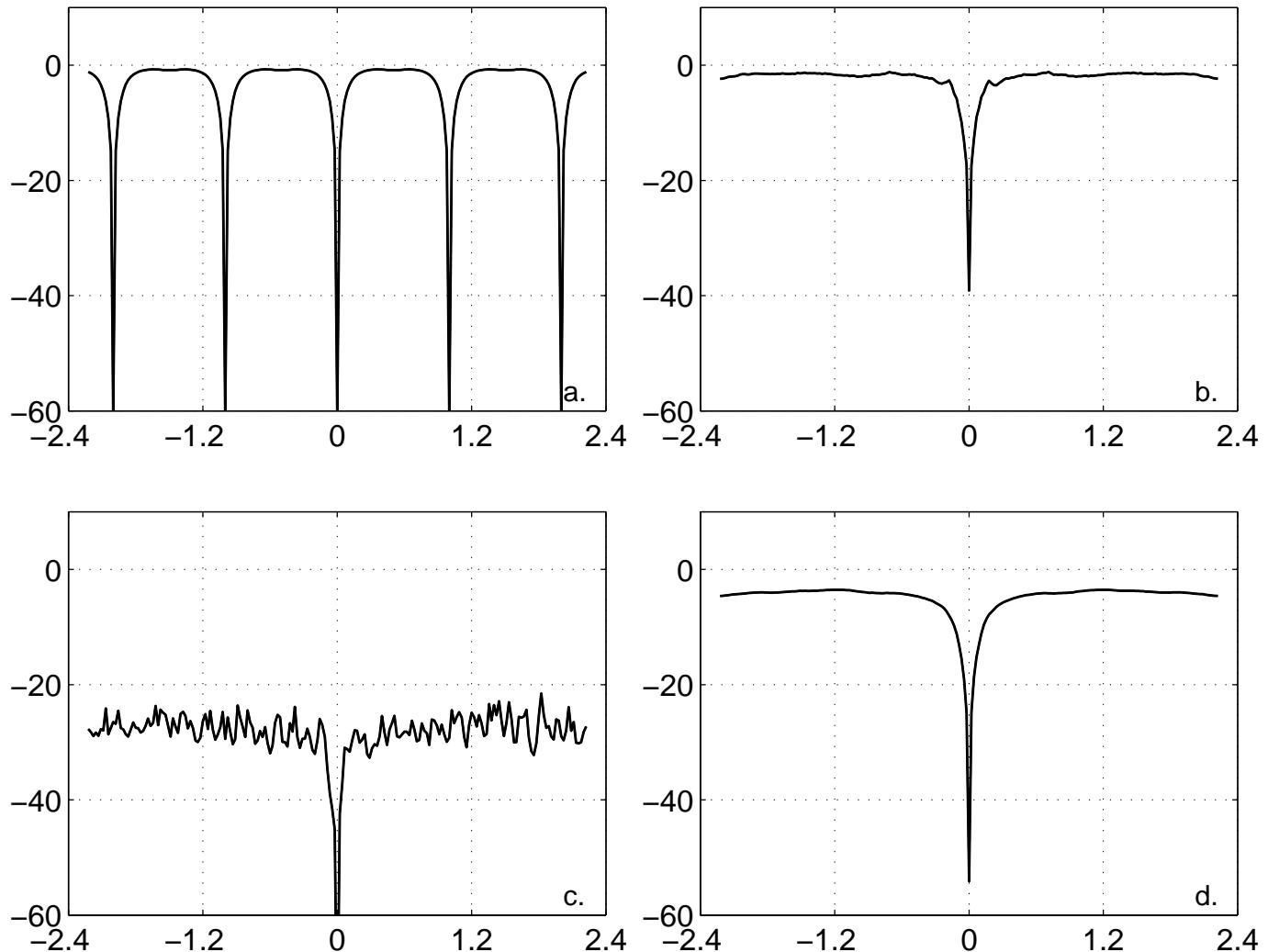
- Avoidance of multiple clutter notches (blind velocities)
- Unambiguous target Doppler estimates
- Resistance against spot jammers
- However: no FFT for Doppler filter bank

## Space-time adaptive FIR filtering with staggered PRI



Matrix scheme for space-time FIR filtering  
( $K=4, M=5, L=3$ )

## Space-time adaptive FIR filtering with staggered PRI



### Space-time FIR filter with staggered PRI

- a. optimum processing, no staggering, Nyquist sampling in space & time
- b. optimum processor, staggered PRI
- c. fixed ST FIR filter, staggered PRI
- d. STAP FIR filter with variable coefficients

## **Space-time adaptive FIR filtering with staggered PRI**

### **Summary**

- **Staggered PRI:** avoiding blind velocities (ambiguous) clutter notches, unambiguous estimation of target Doppler, resistance against spot jammers
- The **optimum (LR) STAP processor** can cope with staggered PRI
- The STAP **FIR filter** is a most efficient tool for real-time clutter rejection
- **FIR** filters with **constant coefficients** are mismatched to staggered echo sequences
- FIR filters with **varying coefficients** (readaption at every PRI)
- **Loss** compared with constant FIR filter and constant PRI: a few dB